

UNIT-III

Mathematics

(INVERSE TRIGONOMETRIC FUNCTIONS)

- 1 Write down the principal value range of $\text{Cos}^{-1}x$ function. 1
- 2 What is the domain of $\text{cosec}^{-1}x$ function ? 1
- 3 Evaluate $\tan^{-1} \sqrt{3} - \sec^{-1}(-2)$ 1
- 4 Find the value of $\cot^{-1}(x) + \cot^{-1}(x)$ when $x < R$. 1
- 5 Write down the value of $\sin^{-1}\{2x\sqrt{1-x^2}\}$ in terms of $\cos^{-1}x$. 1
- 6 Evaluate $\cos\{\sec^{-1}x + \text{cosec}^{-1}x\}$. 1
- 7 What is the principal value of $\sin^{-1}\left\{\sin\frac{3\pi}{5}\right\}$.? 1
- 8 Evaluate $\sin\left\{\frac{\pi}{3} - \sin^{-1}\left(\frac{-1}{2}\right)\right\}$. 1
- 9 Given statement is true or false. ? $\sin^{-1}x = \frac{1}{\sin x}$ 1
- 10 Find x if $\tan^{-1}x + \cot^{-1}4 = \frac{\pi}{2}$. 1
- 11 Evaluate the principal value of
$$\cos^{-1}\left(\frac{\sqrt{3}}{2}\right) \cdot \tan^{-1}x + \tan^{-1}\frac{2x}{1-x^2} = \tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right)$$
 1
- 12 Evaluate $\sin\left\{3\sin^{-1}\frac{2}{5}\right\}$. 1
- 13 Find the value of $\cos\{\sin^{-1}x\}$ in terms of x . 1
- 14 If $\cos^{-1}\frac{1}{x} = \theta$, then write $\tan\theta$ in terms of x . 1
- 15 For what value of x ,
$$\sin\left[\sin^{-1}\frac{1}{5} + \cos^{-1}x\right] = 1$$
 1
- 16 It $\sin x = \frac{\pi}{5}$, then find the value of $\cos^{-1}x$. 1
- 17 Write the value of $\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$. 1
- 18 Write down the simplest form of the function $\tan^{-1}\left(\frac{x-y}{1+xy}\right) + \tan^{-1}y$. 1
- 19 Evaluate –
$$\text{cosec}\left\{\tan^{-1}(-\sqrt{3})\right\}$$
. 1

- 1 Show that $\tan^{-1} \frac{1}{2} + \tan^{-1} \frac{2}{11} = \tan^{-1} \frac{3}{4}$ 1½+1½+1=4
- 2 Prove that $2 \tan^{-1} \frac{1}{2} + \tan^{-1} \frac{1}{7} = \tan^{-1} \frac{31}{17}$ 1+2+1=4
- 3 Prove that $\cos^{-1} \frac{12}{13} + \sin^{-1} \frac{3}{5} = \sin^{-1} \frac{56}{65}$ 1+2+1=4
- 4 Prove that $\tan^{-1} \frac{1}{5} + \tan^{-1} \frac{1}{7} + \tan^{-1} \frac{1}{3} + \tan^{-1} \frac{1}{8} = \pi/4$ 1+1+1+1=4
- 5 Simplify $\tan^{-1} \left(\frac{a \cos x - b \sin x}{b \cos x + a \sin x} \right)$ 1+1+1+1=4
- 6 Simplify $\sin^{-1} \left(\frac{5x + 12\sqrt{1-x^2}}{13} \right)$ 1+1+1+1=4
- 7 Simplify $\tan^{-1} \left(\frac{3a^2x - x^3}{a^3 - 3ax^2} \right)$ 1+1½+1½=4
- 8 Prove that $\cos^{-1} \left(\frac{\sqrt{1+\sin x} + \sqrt{1-\sin x}}{\sqrt{1+\sin x} - \sqrt{1-\sin x}} \right) = \frac{x}{2}$ 1+2+1=4
- 9 Simplify $\tan^{-1} \left(\frac{\cos x}{1-\sin x} \right)$ 2+1+1=4
- 10 Prove that $\frac{9\pi}{8} - \frac{9}{4} \sin^{-1} \frac{1}{3} = \frac{9}{4} \sin^{-1} \frac{2\sqrt{2}}{3}$ 1+2+1=4
- 11 Solve for x $2 \tan^{-1}(\cos x) = \tan^{-1}(2 \operatorname{cosec} x)$ 1+1+2=4
- 12 Solve for x $\tan^{-1} \frac{1-x}{1+x} = \frac{1}{2} \tan^{-1} x$ 2+1+1=4
- 13 Solve for x $\tan^{-1} 2x + \tan^{-1} 3x = \pi/4$ 2+1+1=4
- 14 Write the value of
- (a) $\tan^{-1}(1) + \cos^{-1} \left(\frac{-1}{2} \right) + \sin^{-1} \left(\frac{-1}{2} \right)$ 1/2×4=2
1+1=2
- (b) $\tan^{-1}(\tan(7\pi/6))$
- 15 Prove that $\tan^{-1} x + \tan^{-1} \frac{2x}{1-x^2} = \tan^{-1} \left(\frac{3x-x^3}{1-3x^2} \right)$ 2+1+1=4

(06 marks each)

- 1 Prove that $\tan^{-1} \left(\frac{\sqrt{1+x^2} - \sqrt{1-x^2}}{\sqrt{1+x^2} + \sqrt{1-x^2}} \right) = \frac{\pi}{4} - \frac{1}{2} \cos^{-1} x^2$ 1+1½+1½+
1½+1/2=6
- 2 Simplify a) $\tan^{-1} \left(\frac{\sqrt{1+x^2} - 1}{x} \right)$ 3+3=6

$$\text{b) } \tan^{-1}\left(\frac{1+\cos x}{\sin x}\right)$$

3 Prove that $\tan^{-1}\left(\frac{\pi}{4} + \frac{1}{2}\cos^{-1}\frac{a}{b}\right) + \tan^{-1}\left(\frac{\pi}{4} - \frac{1}{2}\cos^{-1}\frac{a}{b}\right) = \frac{2b}{a}$ 2+2+1+1=6

4 Find the value of x . if

$$\sin^{-1}\left(\frac{2\alpha}{1+\alpha^2}\right) - \cos^{-1}\left(\frac{1-\beta^2}{1+\beta^2}\right) = \tan^{-1}\left(\frac{2x}{1-x^2}\right)$$
 2+2+1+1=6

5 Find the value of

a) $\tan^{-1}\left[2\cos\left(2\sin^{-1}\frac{1}{2}\right)\right]$ 3+3=6

b) $\tan\frac{1}{2}\left[\sin^{-1}\frac{2x}{1+x^2} + \cos^{-1}\frac{1-y^2}{1+y^2}\right]$

6 If $y = \cos^{-1}(\sqrt{\cos x}) - \tan^{-1}(\sqrt{\cos x})$ show that $\sin y = \tan^2 x_2$ 1+2+1+1+1=6

7 i) Write the principal of $\cos^{-1} x$

ii) Write the value of $\cos(\tan^{-1} \alpha + \cos^{-1} \alpha)$

iii) $\sin^{-1} \sqrt{x} + \cos^{-1} \sqrt{x} = \text{-----}$

iv) $\cos(\cos^{-1} x) = \text{-----}$

v) $2 \tan^{-1} = \cos^{-1} = \text{-----}$

vi) Find x if $\sec^{-1} x + \operatorname{cosec}^{-1} 3 = \pi / 2$ 1*6=6

8 a) If $x = \sqrt{a^{\sin^{-1} t}}$ & $y = \sqrt{a^{\cos^{-1} t}}$

Prove that $x^2 y^2 = a^{\pi/2} = \operatorname{cosec} \tan t$.

b) Simplify $\sin^{-1}\left(\frac{3x+4\sqrt{1-x^2}}{5}\right)$ 3+3=6

9 Show that $\sin^{-1}\frac{12}{13} + \cos^{-1}\frac{4}{5} + \tan^{-1}\frac{63}{16} = \pi$ 2+1+2+1=6